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A generic capacitated multi-period, multi-product, integrated forward-reverse logistics network design optimization model

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ABSTRACT: In This Paper, A Generic Capacitated Multi-Product, Multi-Period, Multi-Echelon Integrated Forward-Reverse Logistics Network Design Is Developed. The Proposed Network Structure Consists Of Three Echelons In The Forward Direction, (Suppliers, Factories, And Distributors) And Two Echelons In The Reverse Direction (Disassembly And Redistribution Centers) To Provide The First Customer Zones With Virgin Products And The Second Customer Zones With Refurbished Ones. The Problem Is Formulated In A Mixed Integer Linear Programming (MILP) Decision-Making Form. The Objective Is To Maximize The Total Profit. The Performance Of The Developed Model Has Been Verified Through Two Examples.

KEYWORDS: Supply Chain; Location Allocation; Reverse Logistics; Forward-Reverse Logistics; MILP; Mixed Integer Linear Programming; Closed Loop.

I. INTRODUCTION

Closed loop or integrated forward reverse network establishes a relationship between the market that releases used or refurbished products and the market for new or virgin products.

Salema, M. I. G. et al. (2007) developed a mixed integer formulation for reverse distribution allows for any number of products, <u>But the inventory was not taken into consideration</u>.

Pishvaee, M. S. et al. (2009) developed a <u>single period single product</u> stochastic programming model for an integrated forward/reverse logistics network design under uncertainty.

El-Sayed, M. et al. (2010) developed a <u>single product</u> stochastic mixed integer linear programming for designing a forward–reverse logistics under demand risk.

Ramezani, M. et al. (2013) presented a <u>single period</u> stochastic multi-objective model for forward/reverse logistic network design under an uncertain environment.

Mutha, A., & Pokharel, S. (2013) proposed a mathematical RLN design model considering a third party collectors.

Hatefi, S. M., & Jolai, F. (2014) formulated a <u>single period, single product</u> robust and reliable model for an integrated forward–reverse logistics network design based on a recent robust optimization approach protecting the network against uncertainty.

Serdar E. T. & Al-Ashhab M. S. (2016) modeled a multi-product, multi-period supply chain network mathematically in a mixed integer linear programming (MILP) form deciding both location and allocation decisions which maximize the total profit.

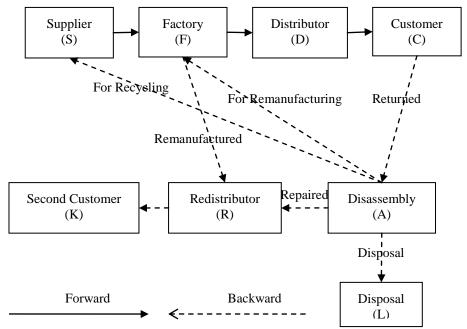
In this work, a generic multi-product, multi-period multi-echelon integrated forward-reverse logistics network design model is developed. The model is formulated in a mixed integer linear programming (MILP) decision-making form. The objective of the model is to maximize the total profit. Decisions are taken to determine the following:

- i. Suppliers, factories, distribution centers, disassembly, and redistribution centers locations,
- ii. Production volume at each period in each location (what and how much to produce),
- iii. Transported quantity of goods between locations, and
- iv. The quantity of goods to hold as inventory at each period in both the facility and distributor stores.

II. MODEL DESCRIPTION

The model is a formulation for the integrated forward-reverse logistics network design problem. The network is a multi-product, multi-period, multi-echelon, where it consists of three suppliers, three factories, three distributors, and four first customers in the forward direction and it consists of three disassembles, three disposal centers, three redistribution locations and second customers in the reverse direction, as shown in Figure 1.

Figure 1: The proposed forward-reverse logistics network



In the forward direction, the suppliers supply the raw material to the factories which manufacture them and send them to the distributors to send them to the first customer considering their demand. In the reverse direction, the first customers return the used products to the disassembly locations for disassembling, and sorting for supplying the recyclable to the suppliers, the remanufacturable to the factories, the disposable to the disposal locations, and to repair the repairable products and supplying them directly to the redistribution locations. The recycled material is supplied to factories. The remanufactured and repaired products are supplied to the second customers through redistribution locations.

Costs incurred at different locations are as follows are shown in Table 1.

Table 1: Costs incurred at different locations of the network

| Forward Logist | ics Echelons Cost Eleme | ents | |
|------------------|-------------------------|--|-------------------|
| Location | Suppliers | Factories | Distributors |
| | 1. Fixed | 1. Fixed | 1. Fixed |
| | 2. Materials | 2. Manufacturing | 2. Shortage |
| | 3. Recycling | 3. Remanufacturing | 3. Storage |
| Costs | 4. Transportation | 4. Non-utilized manufacturing capacity | 4. Transportation |
| | | 5. Non-utilized remanufacturing capacity | |
| | | 6. Storage | |
| | | 7. Transportation | |
| Reverse Logistic | cs Echelons Cost Elemen | nts | |
| Location | Disassembly | Redistribution | Disposal |
| | 1. Fixed | 1. Fixed | 1. Fixed |
| | 2. Returned price | 2. Transportation | 2. Disposing |
| | 3. Disassembly | | |
| Costs | 4. Inspection | | |
| | 5. Sorting | | |
| | 6. Repairing | | |
| | 7. Transportation | | |

III. MODEL FORMULATION

The model involves the following sets, parameters, and decision variables: **Sets:**

S, F, D, and C: potential number of suppliers, factories, distributors, and first customers,

A, R, L, and K: potential number of disassembly, redistributors, locations, disposal, and second customers.

P: number of products,

T: number of periods.

Parameters:

Dcpt: demand of first customer c from product p in period t,

Dkpt: demand of the second customer k from product p in period t,

Ppct: unit price of product p at customer c in period t,

Ppkt: unit price of product p at second customer k in period t,

Fi: fixed cost of opening location i,

DSij: distance between any two locations i and j,

CAPSst: capacity of supplier s in period t (kg),

CAPMft: capacity of raw material store of facility f in period t (kg),

CAPHft: capacity in manufacturing hours of facility f in period t,

CAPFSft: capacity of final product store of facility f in period t (kg),

CAPDdt: capacity of distributor d in period t (kg),

CAPAat: capacity of disassembly a in period t,

CAPRCst: recycling capacity of supplier s in period t (kg),

CAPRMft: remanufacturing capacity in hours of factory f in period t,

CAPRrt: capacity of redistributor r in period t,

CAPLIT: capacity of disposal p in period t,

MatCst: material cost per unit supplied by supplier s in period t,

RECst: recycling cost per unit recycled by supplier s in period t,

MCft: manufacturing cost per hour for factory *f* in period *t*,

RMCft: remanufacturing cost per hour for factory f in period t,

DACat: disassembly cost per unit weight disassembled by disassembly location a in period t,

REPCat: repairing cost per unit repaired by disassembly location a in period t,

DISPClt: disposal cost per unit disposed of by disposal location l in period t,

NUCCf: non-utilized manufacturing capacity cost per hour of facility f,

NURCCf: non-utilized remanufacturing capacity cost per hour of factory f,

SCPUp: shortage cost per unit per period for product p,

MHp: manufacturing hours for product p,

RMHp: remanufacturing hours for product p,

FHf: holding cost per unit weight per period at the store of factory f,

DHd: holding cost per unit weight per period at distributor store d,

Bs, Bf, Bd, Ba & Br: batch size from supplier s, factory f, distributor d, disassembly a, and, redistributor r respectively,

Tc: transportation cost per unit per kilometer,

RR: return ratio at the first customers,

RC: recycling ratio,

RM: remanufacturing ratio,

RP: repairing ratio,

RD: disposal ratio,

Decision variables:

Li: binary variable equals 1 if location i is open and 0 otherwise,

Qijpt: flow of batches from location i to location j of product p in period t,

Ifpt: flow of batches from factory f to its store of product p in period t,

Ifdpt: flow of batches from store of factory f to distributor d of product p in period t,

Rfpt: the residual inventory of product p in the period t at store of factory f,

Rdpt: the residual inventory of product p in the period t at distributor d.

3.1. Objective Function

The objective of the model is to maximize the total profit of the forward-reverse network.

Total Profit = Total Revenue – Total Cost.

3.1.1. Total Revenue

Total Revenue = First Sales + Second Sales + Recycling Cost Saving.

First Sales =
$$\sum_{d \in D} \sum_{c \in C} \sum_{p \in P} \sum_{t \in T} Q_{dcpt} B_{dp} P_{pct}$$
 (1)

Second Sales
$$= \sum_{r \in R} \sum_{k \in C} \sum_{p \in P} \sum_{r \in T} Q_{rkpt} B_{rp} P_{pkt}$$
 (2)

Recycling cost saving
$$= \sum_{a \in A} \sum_{s \in S} \sum_{p \in P} \sum_{t \in T} Q_{ast} B_a W_p (MatC_{st} - REC_{st})$$
 (3)

3.1.2. Total Cost

Total cost = fixed costs + material costs + manufacturing costs + non-utilized capacity costs + shortage costs + Purchasing costs + Disassembly costs + Remanufacturing cost + Repairing cost + Disposal cost + Transportation costs + inventory holding costs.

The costs are as follows:

1) Fixed Costs

$$\sum_{s \in S} F_s L_s + \sum_{f \in F} F_f L_f + \sum_{d \in D} F_d L_d + \sum_{a \in A} F_a L_a + \sum_{r \in R} F_r L_r + \sum_{l \in L} F_l L_l \tag{4}$$

2) Material Cost

$$\sum_{s \in S} \sum_{f \in F} \sum_{t \in T} Q_{sft} B_s MatC_{st}$$
(5)

3) Manufacturing Costs

$$\sum_{f \in F} \sum_{d \in D} \sum_{p \in P} \sum_{t \in T} Q_{\text{fdpt}} B_{\text{fp}} MH_{p} MC_{\text{ft}} + \sum_{f \in F} \sum_{d \in D} \sum_{p \in P} \sum_{t \in T} I_{\text{fpt}} B_{\text{fp}} MH_{p} MC_{\text{ft}}$$

$$(6)$$

4) Non-Utilized Manufacturing Capacity Cost (for factories)

$$\sum_{f \in F} \left(\sum_{t \in T} \left((CAPH_{ft}) L_{f} - \sum_{d \in D} \sum_{p \in P} (Q_{ftpt} B_{fp} MH_{p}) - \sum_{d \in D} \sum_{p \in P} (I_{ftpt} B_{fp} MH_{p}) \right) NUCC_{f} \right)$$

$$\sum_{f \in F} \left(\sum_{p \in P} \sum_{t \in T} \left((CAPH_{ft}) L_{f} - \sum_{d \in D} (Q_{ftpt} B_{fp} MH_{p}) - \sum_{d \in D} (I_{ftpt} B_{fp} MH_{p}) \right) NUCC_{f} \right)$$

$$(7)$$

5) Shortage Cost (for distributor)

$$\sum_{p \in P} \left(\sum_{c \in C} \left(\sum_{t \in T} \left(\sum_{t}^{t} DEMAND - \sum_{cpt}^{t} - \sum_{d \in D} Q_{dcpt} B_{dp} \right) \right) \right) SCPU_{p}$$
(8)

6) Purchasing Cost

$$\sum_{c \in C} \sum_{a \in A} \sum_{p \in P} \sum_{t \in T} Q_{capt} P_{pct} B_c QL_c$$

$$(9)$$

7) Disassembly Costs

$$\sum_{c \in C} \sum_{a \in A} \sum_{p \in P} \sum_{t \in T} Q_{capt} B_c DAC_{at}$$
(10)

8) Non-Utilized Remanufacturing Capacity Cost (for factories)

$$\sum_{f \in F} \left(\sum_{t \in T} \left(\left(CAPRM - \sum_{f \in R} \sum_{p \in P} \left(Q_{fipt} - B_{fip} - RMH - \sum_{p} \right) \right) NURCC - C \right)$$

$$(11)$$

9) Remanufacturing Costs

$$\sum_{f \in F} \sum_{r \in R} \sum_{p \in P} \sum_{t \in T} Q_{fipt} B_{fp} RMH PRMC$$
(12)

10) Repairing Costs

$$\sum_{a \in A} \sum_{r \in R} \sum_{p \in P} \sum_{t \in T} Q_{arpt} B_a W_p REPC$$
(13

11) Disposal Costs

$$\sum_{a \in A} \sum_{l \in L} \sum_{p \in P} \sum_{t \in T} Q_{alpt} B_a W_p DISPC$$
(14

12) Transportation Costs

$$\sum_{\mathsf{t} \in \mathsf{T}} \sum_{\mathsf{s} \in \mathsf{S}} \sum_{\mathsf{f} \in \mathsf{F}} \mathsf{Q}_{\mathsf{sft}} \; \; \mathsf{B}_{\mathsf{s}} \; \mathsf{T}_{\mathsf{s}} \; \; \mathsf{DS}_{\mathsf{sf}} \; \; + \sum_{\mathsf{t} \in \mathsf{T}} \sum_{\mathsf{f} \in \mathsf{F}} \sum_{\mathsf{d} \in \mathsf{D}} \sum_{\mathsf{p} \in \mathsf{P}} \mathsf{Q}_{\mathsf{idpt}} \; \; \mathsf{B}_{\mathsf{f}} \; \mathsf{W}_{\mathsf{p}} \; \; \mathsf{Tc} \; \; \mathsf{DS}_{\mathsf{id}} \; \; + \sum_{\mathsf{t} \in \mathsf{T}} \sum_{\mathsf{f} \in \mathsf{F}} \sum_{\mathsf{d} \in \mathsf{D}} \sum_{\mathsf{p} \in \mathsf{P}} \mathsf{I}_{\mathsf{idpt}} \; \; \mathsf{B}_{\mathsf{fp}} \; \mathsf{W}_{\mathsf{p}} \; \mathsf{T}_{\mathsf{f}} \; \; \mathsf{D}_{\mathsf{id}} \; (1 + SN) \;) \; + \; \mathsf{D}_{\mathsf{f}} \; \; \mathsf{D}_{\mathsf$$

$$\sum_{d \in D} \sum_{c \in C} \sum_{p \in P} \sum_{t \in T} Q_{dept} B_{dp} W_{p} T_{d} D_{dc} + \sum_{t \in T} \sum_{d \in D} \sum_{a \in A} \sum_{s \in S} Q_{aspt} B_{a} W_{p} Tc DS_{as} + \sum_{t \in T} \sum_{d \in D} \sum_{a \in A} \sum_{f \in F} Q_{aipt} B_{a} W_{p} Tc DS_{af}$$

$$\sum_{t \in T} \sum_{d \in D} \sum_{f \in F} \sum_{r \in R} Q_{fipt} B_{f} W_{p} Tc DS_{fi} + \sum_{t \in T} \sum_{d \in D} \sum_{a \in A} \sum_{r \in R} Q_{aspt} B_{a} W_{p} Tc DS_{ar} + \sum_{t \in T} \sum_{d \in D} \sum_{a \in A} \sum_{I \in L} Q_{alpt} B_{a} W_{p} Tc DS_{al} + \sum_{t \in T} \sum_{d \in D} \sum_{a \in A} \sum_{I \in L} Q_{alpt} B_{a} W_{p} Tc DS_{al} + \sum_{t \in T} \sum_{d \in D} \sum_{a \in A} \sum_{I \in L} Q_{alpt} B_{a} W_{p} Tc DS_{al} + \sum_{t \in T} \sum_{d \in D} \sum_{a \in A} \sum_{I \in L} Q_{alpt} B_{a} W_{p} Tc DS_{al} + \sum_{t \in T} \sum_{d \in D} \sum_{a \in A} \sum_{I \in L} Q_{alpt} B_{a} W_{p} Tc DS_{al} + \sum_{t \in T} \sum_{d \in D} \sum_{a \in A} \sum_{I \in L} Q_{alpt} B_{a} W_{p} Tc DS_{al} + \sum_{t \in T} \sum_{d \in D} \sum_{a \in A} \sum_{I \in L} Q_{alpt} B_{a} W_{p} Tc DS_{al} + \sum_{t \in T} \sum_{d \in D} \sum_{a \in A} \sum_{I \in L} Q_{alpt} B_{a} W_{p} Tc DS_{al} + \sum_{t \in T} \sum_{d \in D} \sum_{a \in A} \sum_{I \in L} Q_{alpt} B_{a} W_{p} Tc DS_{al} + \sum_{t \in T} \sum_{d \in D} \sum_{a \in A} \sum_{I \in L} Q_{alpt} B_{a} W_{p} Tc DS_{al} + \sum_{t \in T} \sum_{d \in D} \sum_{a \in A} \sum_{I \in L} Q_{alpt} B_{a} W_{p} Tc DS_{al} + \sum_{t \in T} \sum_{d \in D} \sum_{a \in A} \sum_{I \in L} Q_{alpt} B_{a} W_{p} Tc DS_{al} + \sum_{t \in T} \sum_{d \in D} \sum_{a \in A} \sum_{I \in L} Q_{alpt} B_{a} W_{p} Tc DS_{al} + \sum_{t \in T} \sum_{d \in D} \sum_{a \in A} \sum_{I \in L} Q_{alpt} B_{a} W_{p} Tc DS_{al} + \sum_{t \in T} \sum_{d \in D} \sum_{a \in A} \sum_{I \in L} Q_{alpt} B_{a} W_{p} Tc DS_{al} + \sum_{t \in T} \sum_{d \in D} \sum_{a \in D} \sum$$

$$\sum_{\mathsf{t} \in \mathsf{T}} \sum_{d \in D} \sum_{\mathsf{r} \in R} \sum_{k \in K} \mathsf{Q}_{\mathsf{rkpt}} \; \mathsf{B}_{\mathsf{r}} \mathsf{W}_{\mathsf{p}} \; \mathsf{Tc} \; \mathsf{DS}_{\mathsf{rk}}$$

13) Inventory Holding Costs

$$\sum_{p \in P} \left(\sum_{f \in F} \sum_{t \in T} R_{fpt} W_{p} HF_{f} + \sum_{d \in D} \sum_{t \in T} R_{dpt} W_{p} HD_{d} \right)$$

$$(16)$$

3.2. Constraints

This section is a representation of the constraints of the model:

3.2.1. Balance Constraints:

Balance constraints at for factories, stores, distributors, disassembly, and redistributors locations are given in the following equations (17-29).

3.2.1.1 Factory balance

$$\sum_{s \in S} Q_{sft} B_s = \sum_{d \in D} \sum_{p \in P} Q_{fdpt} B_{fp} W_p + I_{fpt} B_{fp} W_p, \forall t \in T, \forall f \in F$$

$$(17)$$

3.2.1.2 Factory store balance

$$I_{fpt} B_{fp} + R_{fp(t-1)} B_{fp} = R_{fpt} B_{fp} + \sum_{d \in D} I_{fdpt} B_{fp}, \forall t \in T, \forall f \in F, \forall p \in P$$
(18)

3.2.1.3 Distributor store balance

$$\sum_{f \in F} (Q_{fdpt} + I_{fdpt}) B_{fp} + R_{dp(t-1)} B_{dp} = R_{dpt} B_{dp} + \sum_{c \in C} Q_{dcpt} B_{dp}, \forall t \in 2 \to T, \forall d \in D, \forall p \in P$$
(19)

3.2.1.4 Customer in balance

$$\sum_{d \in D} Q_{dcpt} B_{dp} \leq \text{DEMAND} \qquad _{cpt} + \sum_{1 \to t} \text{DEMAND} \qquad _{cp (t-1)} - \sum_{d \in D} Q_{dcp (t-1)} B_{dp}, \forall t \in T, \forall c \in C, \forall p \in P$$

$$(20)$$

3.2.1.5 Customer out balance

$$\sum_{a \in A} Q_{capt} B_{c} \le \left(\sum_{d \in D} Q_{dcpt} B_{d}\right) RR, \forall t \in T, \forall c \in C, \forall p \in C, \forall p \in P$$
(21)

3.2.1.6 Disassembly balance

$$\sum_{c \in C} Q_{capt} B_{c} = \sum_{s \in S} (Q_{aspt} B_{a}) + \sum_{f \in F} (Q_{afpt} B_{a}) + \sum_{f \in R} (Q_{arpt} B_{a}) + \sum_{l \in L} (Q_{alpt} B_{a}), \forall t \in T, \forall a \in A, \forall p \in P$$
(22)

3.2.1.7 Recycling balance

$$\sum_{c \in C} (Q_{capt} \mid B_c \mid RC) = \sum_{s \in S} (Q_{aspt} \mid B_a), \forall t \in T, \forall a \in A, \forall p \in P$$
(23)

3.2.1.8 Remanufacturing balance

$$\sum_{c \in C} (Q_{capt} B_c RM) = \sum_{f \in F} (Q_{afpt} B_a), \forall t \in T, \forall a \in A, \forall p \in P$$
(24)

3.2.1.9 Return balance

$$\sum_{c \in C} (Q_{capt} \mid B_c \mid RP) = \sum_{r \in R} (Q_{apt} \mid B_a), \forall t \in T, \forall a \in A, \forall p \in P$$
(25)

3.2.1.10 Disposing balance

$$\sum_{c \in C} (Q_{capt} \mid B_c \mid RD) = \sum_{l \in L} (Q_{alpt} \mid B_a), \forall t \in T, \forall a \in A, \forall p \in P$$
(26)

3.2.1.11 Remanufacturing balance

$$\sum_{a \in A} (Q_{afpt} \mid B_a) = \sum_{f \in R} (Q_{fpt} \mid B_f), \forall f \in T, \forall f \in F, \forall p \in P$$

$$(27)$$

3.2.1.12 Redistribution balance

$$\sum_{a \in A} (Q_{arpt} B_a) + \sum_{f \in F} (Q_{frpt} B_f) = \sum_{k \in K} (Q_{rkpt} B_r), \forall t \in T, \forall r \in R, \forall p \in P$$

$$(28)$$

3.2.1.13 Second customer balance

$$\sum_{r \in R} (Q_{rkpt} \mid B_r) \le D_{kpt}, \forall t \in T, \forall k \in K, \forall p \in P$$
(29)

3.2.2. Capacity Constraints:

Capacity constraints for suppliers, factories, stores, distributors, disassembly, disposal, and redistributors locations are given in the following equations (30-38)

3.2.2.1 Supplier capacity

$$\sum_{f \in F} Q_{sft} B_s \le CAPS_{st} L_s, \forall t \in T, \forall s \in S$$
(30)

3.2.2.2 Factory material capacity

$$\sum_{s \in S} Q_{sft} B_s \le CAPM \quad _{ft} L_f, \forall t \in T, \forall f \in F$$
(31)

3.2.2.3 Manufacturing hours capacity

$$\left(\sum_{d \in D} Q_{\text{filpt}} B_{\text{fip}} + \sum_{d \in D} I_{\text{fipt}} B_{\text{fip}}\right) MH_{p} \leq CAPH_{\text{fi}} L_{f}, \forall t \in T, \forall f \in F, \forall p \in P$$
(32)

3.2.2.4 Facility store capacity

$$\sum_{p \in P} R_{\text{fpt}} B_{\text{fp}} W_{p} \leq \text{CAPFS} \quad _{\text{ft}} L_{f}, \forall t \in T, \forall f \in F$$
(33)

3.2.2.5 Distributor store capacity

$$\sum_{f \in F} \sum_{p \in P} (Q_{\text{filpt}} + I_{\text{filpt}}) B_{\text{fip}} W_p + \sum_{p \in P} R_{\text{dpt-1}} B_{\text{dp}} W_p \leq CAPD_{\text{dt}} L_d, \forall t \in T, \forall d \in D$$

$$(34)$$

3.2.2.6 Disassembly capacity

$$\sum_{s \in S} \sum_{p \in P} Q_{aspt} B_a W_p + \sum_{f \in F} \sum_{p \in P} Q_{afpt} B_a W_p + \sum_{r \in R} \sum_{p \in P} Q_{arpt} B_a W_p + \sum_{f \in F} \sum_{p \in P} Q_{alpt} B_a W_p \le CAPA_{lt}, \forall t \in T, \forall a \in A$$

$$(35)$$

3.2.2.7 Redistributors capacity

$$\sum_{k \in K} \sum_{p \in P} Q_{rkpt} B_r W_p \le CAPR_{rt}, \forall t \in T, \forall r \in R$$
(36)

3.2.2.8 Recycling capacity

$$\sum_{a \in A} \sum_{p \in P} Q_{aspt} B_a W_p \le CAPRC \quad st, \forall t \in T, \forall s \in S$$
(37)

3.2.2.9 Disposal capacity

$$\sum_{a \in A} \sum_{p \in P} Q_{alpt} B_a W_p \le PC_{pt}, \forall t \in T, \forall l \in L$$
(38)

The model is built by using Mosel language [8], which can be work as both a modeling language and a programming language.

IV. MODEL VERIFICATION RESULTS ANALYSIS

The effectiveness of the model has been verified through solving two examples with different demand patterns. Other parameters are assumed to be constant and having the values given in Table 2.

Table 2: Nominal values of the model parameters

| Parameter | Value | Parameter | Value |
|---|------------------|--|--------|
| Virgin products prices | 100, 150 and 200 | Supplier locations fixed costs. | 10,000 |
| Weights of the three products | 1, 2 and 3 Kg. | Factory location fixed costs. | 50,000 |
| Manufacturing time of each product | 1, 2 and 3 hr. | Distributor locations fixed costs. | 5,000 |
| Remanufacturing time of each product | 2, 3 and 4 hr. | Disassembly location fixed costs. | 2,000 |
| Second customer demand for each product in each period | 500 | Redistribution location fixed costs. | 2,000 |
| Second products price ratio | 80 % | Disposal location Fixed costs. | 1,000 |
| Returned products quality (may be random) | 20 % | Supplier recycling capacity (kg) | 2,000 |
| Material cost per kilogram | 10 | Supplier capacity (kg) | 4,000 |
| Manufacturing costs per unit | 10 | Factory store capacity | 2,000 |
| Shortage cost for each product per period | 5, 10 and 15 | Factory raw material storing capacity (kg) | 4,000 |
| Non-Utilized manufacturing capacity cost | 10 | Factory manufacturing capacity (hours) | 6,000 |
| Non-Utilized remanufacturing capacity cost | 10 | Factory remanufacturing capacity (hours) | 2,000 |
| Factory holding cost | 3 | Distributor store capacity | 4,000 |
| Distributor holding cost | 2 | Disassembly location capacity | 2,000 |
| Disassembly cost per unit | 3 | Redistribution capacity | 2,000 |
| Recycling cost per unit | 5 | Disposal location capacity | 1,000 |
| Remanufacturing cost per unit | 10 | Max return ratio | 50 % |
| Repairing cost | 5 | Repairing ratio | 50% |
| Disposal cost | 1 | Recycling ratio | 10% |
| Max number of operating suppliers, factories, distributors, disassembles and redistributors | 3 | Remanufacturing ratio | 30% |
| Max number of first customers | 4 | Disposal ratio | 10% |
| Max number of second customers | 2 | Batch sizes | 1 |

4.1 EXAMPLE 1

4.1.1 EXAMPLE 1: INPUTS

The model has been verified through the following case study where the input parameters are considered as showing in Table 2. The demand patterns are assumed for all customers as shown in Table 3.

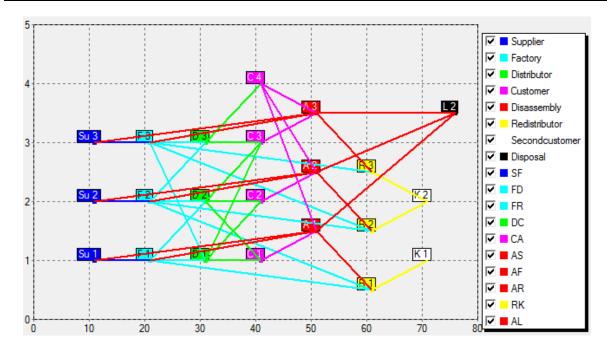
Table 3: Demand of each customer in each period for each product.

| | Required Demand | | | | | | | | | | | |
|----------|-----------------|---------|-----|------------|-----|-----|------------|-----|-----|------------|-----|-----|
| Period | C | ustomer | · 1 | Customer 2 | | | Customer 3 | | | Customer 4 | | |
| 1 er iou | P1 | P2 | P3 | P1 | P2 | P3 | P1 | P2 | P3 | P1 | P2 | P3 |
| 1 | 470 | 500 | 530 | 470 | 500 | 530 | 470 | 500 | 530 | 470 | 500 | 530 |
| 2 | 460 | 490 | 520 | 460 | 490 | 520 | 460 | 490 | 520 | 460 | 490 | 520 |
| 3 | 450 | 480 | 510 | 450 | 480 | 510 | 450 | 480 | 510 | 450 | 480 | 510 |

4.1.2 EXAMPLE 1: OUTPUTS AND DISCUSSION

The resulted optimal network is as shown in Figure 2.

Figure 2: The resulted optimal network of example 1.



Total profit, total cost, total revenue, and their elements are given in Table 4. Only the Inventory Holding Cost equals zero which means that there is no inventory at all in the network.

Table 4: Total profit, total cost, total revenue, and their elements.

| Revenue | Value | Cost | Value | Cost | Value |
|------------------|-----------|------------------------|------------|----------------------|---------|
| First Sales | 2,682,000 | Fixed Cost | 206,500 | Purchasing Costs | 268,200 |
| Second Sales | 858,240 | Material Cost | 360,000 | Disassembly Cost | 54,000 |
| Recycling Profit | 4,410 | Manufacturing Cost | 364,800 | Remanufacturing Cost | 80,460 |
| | | Non-Utilized Cost | 274,740 | Repairing Cost | 45,000 |
| | | Shortage Cost | 2,400 | Disposal Cost | 1,800 |
| | | Inventory Holding Cost | 0 | Transportation Costs | 29,060 |
| Total Revenue | 3,544,650 | 7 | Total Cost | 1,686,960 | |
| | | Total Profit | 1,857,690 | | |

Where the quantities of batches transferred from suppliers to the factories and from factories to distributors are shown in Table 5. Flow balancing is noticed in Table 5 where the total weights of transferred materials are the same of 36000 kg.

Table 5: Number of batches transferred from suppliers and factories.

| From | Suppliers | | | Factories | | | | | | | | |
|----------|-----------|-------|-------|-----------|------|------|-----|-------|------|-----------|------|------|
| FIOIII | S1 | S2 | S3 | F1 | | | F2 | | | F3 | | |
| Period | RM | RM | RM | P1 | P2 | P3 | P1 | P2 | P3 | P1 | P2 | P3 |
| 1 | 4000 | 4000 | 4000 | 940 | 735 | 530 | 1 | 744 | 837 | 919 | 501 | 693 |
| 2 | 4000 | 4000 | 4000 | 460 | 990 | 520 | 460 | 120 | 1100 | 940 | 750 | 520 |
| 3 | 4000 | 4000 | 4000 | 900 | 785 | 510 | 347 | 775 | 701 | 553 | 480 | 829 |
| Weight | 12000 | 12000 | 12000 | 2300 | 5020 | 4680 | 808 | 3278 | 7914 | 2412 | 3462 | 6126 |
| Total W. | | 36000 | | | | | | 36000 | | | | |

The number of batches transferred from distributors to customers for all products in all period of also 36000 kg is shown in Table 6.

Table 6: Number of batches transferred from distributors to customers.

| | Given Quantities | | | | | | | | | | | |
|----------------------|------------------|---------|------------|------------|------|------|------------|------|------|------------|------|------|
| Period | Cı | ustomei | r 1 | Customer 2 | | | Customer 3 | | | Customer 4 | | |
| Periou | P1 | P2 | P3 | P1 | P2 | Р3 | P1 | P2 | P3 | P1 | P2 | P3 |
| 1 | 470 | 500 | 530 | 470 | 490 | 470 | 470 | 490 | 530 | 450 | 500 | 530 |
| 2 | 460 | 490 | 520 | 460 | 500 | 580 | 460 | 380 | 520 | 480 | 490 | 520 |
| 3 | 450 | 480 | 510 | 450 | 480 | 510 | 450 | 600 | 510 | 450 | 480 | 510 |
| Weight (Kg.) | 1380 | 2940 | 4680 | 1380 | 2940 | 4680 | 1380 | 2940 | 4680 | 1380 | 2940 | 4680 |
| Total Weights | | 36000 | | | | | | | | | | |

The shortage can be calculated easily by subtracting given quantities shown in Table 6 from the required quantities (demand) shown in Table 3 and it is shown in Table 7. Table 7 shows that all shortages are compensated in the next periods and these shortages resulted in a shortage cost of 2400 as shown in Table 4.

Table 7: Shortages.

| Shortage per period | | | | | | | | | | | | |
|----------------------|----|---------|----|------------|-----|-----|------------|------|----|------------|----|----|
| Period | Cı | ustomei | :1 | Customer 2 | | | Customer 3 | | | Customer 4 | | |
| reriou | P1 | P2 | Р3 | P1 | P2 | Р3 | P1 | P2 | Р3 | P1 | P2 | P3 |
| 1 | 0 | 0 | 0 | 0 | 10 | 60 | 0 | 10 | 0 | 20 | 0 | 0 |
| 2 | 0 | 0 | 0 | 0 | -10 | -60 | 0 | 110 | 0 | -20 | 0 | 0 |
| 3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | -120 | 0 | 0 | 0 | 0 |
| Weight (Kg.) | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| Total Weights | | 0 | | | | | | | | | | |

Figure 3 depicts the given quantities versus demand for all customer and all products. It can be noticed that they are all equal which means that there are no final shortages. Figure 4 shows that the total required weights are more than the network capacity in the first period equals it at the second period, and less than it at the third period which explains shortage compensation.

Figure 3: Given quantities versus demand for all customer and all products.

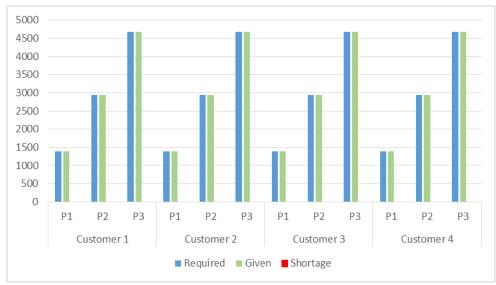
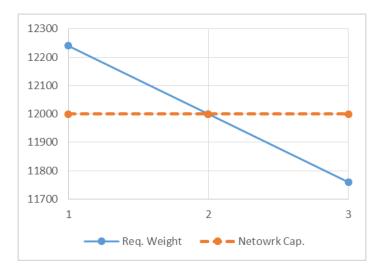


Figure 4: Total required weights vs. network capacity



The flow in the reverse direction begins by receiving the returned products from the first customers by disassembly locations. Table 8 gives the maximum flow weights and the actual flow weights. It is noticed that the disassembly locations receives the maximum flow weights of 18000 kg. So, other actual weights of the repaired, recycled, remanufactured, disposed and redistributed equal the maximum flow weights. The number of products of 18000 kg weight purchased by disassembly locations from the first customers is shown in Table 9.

Table 8: Maximum and actual flow weights.

| | Ratio | Max. fl | ow weights | Actual flow weights | | | |
|----------------|-------|---------|------------|---------------------|-------|--|--|
| Returned | 0.5 | 1 | 8000 | 18000 | | | |
| Redistributed | 0.8 | 1 | 4400 | 14400 | | | |
| Repaired | 0.5 | 9000 | | 9000 | | | |
| Recycled | 0.1 | 1800 | 18000 | 1800 | 18000 | | |
| Remanufactured | 0.3 | 5400 | 18000 | 5400 | 18000 | | |
| Disposed | 0.1 | 1800 | | 1800 | | | |

Table 9: Number of products purchased by disassembly locations from the first customers.

| | • | • | Retune | ed Quar | tities | | | | | |
|----------|-----|-----------|--------|---------|-----------|-----|------|------|-----|--|
| To | | A1 | | | A2 | | | A3 | | |
| Period | | C1A1 | | C1A2 | | | C1A3 | | | |
| Period | P1 | P2 | P3 | P1 | P2 | P3 | P1 | P2 | P3 | |
| 1 | 235 | 250 | 265 | 0 | 0 | 0 | 0 | 0 | 0 | |
| 2 | 230 | 245 | 260 | 0 | 0 | 0 | 0 | 0 | 0 | |
| 3 | 225 | 240 | 255 | 0 | 0 | 0 | 0 | 0 | 0 | |
| Dowlad | | C2A1 | | | C2A2 | | | C2A3 | | |
| Period | P1 | P2 | Р3 | P1 | P2 | Р3 | P1 | P2 | Р3 | |
| 1 | 0 | 0 | 0 | 235 | 245 | 235 | 0 | 0 | 0 | |
| 2 | 0 | 0 | 0 | 230 | 250 | 290 | 0 | 0 | 0 | |
| 3 | 0 | 0 | 0 | 225 | 240 | 255 | 0 | 0 | 0 | |
| Period | | C3A1 | | C3A2 | | | | C3A3 | | |
| 1 er iou | P1 | P2 | P3 | P1 | P2 | P3 | P1 | P2 | P3 | |
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 235 | 245 | 265 | |
| 2 | 0 | 0 | 0 | 0 | 0 | 0 | 230 | 190 | 260 | |
| 3 | 0 | 0 | 0 | 0 | 0 | 0 | 225 | 300 | 255 | |
| Period | | C4A1 | | | C4A2 | | | C4A3 | | |
| reriou | P1 | P2 | P3 | P1 | P2 | P3 | P1 | P2 | P3 | |
| 1 | 55 | 80 | 85 | 105 | 165 | 45 | 65 | 5 | 135 | |
| 2 | 0 | 25 | 150 | 0 | 200 | 0 | 240 | 20 | 110 | |
| 3 | 45 | 160 | 55 | 175 | 80 | 65 | 5 | 0 | 135 | |

| Weight (Kg.) | 790 | 2000 | 3210 | 970 | 2360 | 2670 | 1000 | 1520 | 3480 |
|---------------|-----|------|------|-----|-------|------|------|------|------|
| Total Weights | | | | | 18000 | | | | |

The number and weights of remanufactured, repaired, and delivered to the second customers matching Table 8 are presented in Tables 10, 11 and 12 respectively.

Table 10: Flow of remanufactured products from factories to redistributors.

| | | Remanufactured | | | | | | | | | | |
|----------------------|-----|----------------|------|-----|------|------|----|----|----|--|--|--|
| Period | | F1R | | | F2R | F3R | | | | | | |
| Periou | P1 | P2 | P3 | P1 | P2 | P3 | P1 | P2 | P3 | | | |
| 1 | 99 | 127 | 149 | 180 | 170 | 160 | 0 | 0 | 0 | | | |
| 2 | 129 | 109 | 151 | 150 | 170 | 168 | 0 | 0 | 2 | | | |
| 3 | 85 | 120 | 161 | 185 | 186 | 145 | 0 | 0 | 0 | | | |
| Weight (Kg.) | 313 | 712 | 1383 | 515 | 1052 | 1419 | 0 | 0 | 6 | | | |
| Total Weights | | 5400 | | | | | | | | | | |

Table 11: Flow of repaired products from disassembly locations to redistributors.

| | | Repaired | | | | | | | | | |
|---------------|-----|----------|------|-----|------|------|-----|-----|------|--|--|
| Period | | A1R | | | A2R | | A3R | | | | |
| renou | P1 | P2 | P3 | P1 | P2 | P3 | P1 | P2 | P3 | | |
| 1 | 145 | 165 | 175 | 170 | 205 | 140 | 150 | 125 | 200 | | |
| 2 | 115 | 135 | 205 | 115 | 225 | 145 | 235 | 105 | 185 | | |
| 3 | 135 | 200 | 155 | 200 | 160 | 160 | 115 | 150 | 195 | | |
| Weight (Kg.) | 395 | 1000 | 1605 | 485 | 1180 | 1335 | 500 | 760 | 1740 | | |
| Total Weights | | | | | 9000 | | | | | | |

The number of batches transferred to the second customer through the reverse chain is shown in Table 12.

Table 12: Flow of refurbished products from redistributors to second customers.

| Table 12: Flow of refurbished products from redistributors to second customers. | | | | | | | | | | | |
|---|-----|----------|---------|------|------|------|--|--|--|--|--|
| | | Second P | roducts | | | | | | | | |
| To | | K1 | | | K2 | | | | | | |
| Dowlad | | R1K1 | | | R1K2 | | | | | | |
| Period | P1 | P2 | Р3 | P1 | P2 | Р3 | | | | | |
| 1 | 244 | 292 | 324 | 0 | 0 | 0 | | | | | |
| 2 | 244 | 244 | 356 | 0 | 0 | 0 | | | | | |
| 3 | 220 | 320 | 316 | 0 | 0 | 0 | | | | | |
| Donie d | | R2K1 | | | R2K2 | | | | | | |
| Period | P1 | P2 | Р3 | P1 | P2 | Р3 | | | | | |
| 1 | 0 | 0 | 0 | 350 | 375 | 300 | | | | | |
| 2 | 0 | 0 | 0 | 265 | 395 | 313 | | | | | |
| 3 | 0 | 0 | 0 | 385 | 346 | 305 | | | | | |
| Dowlad | | R3K1 | | | R3K2 | | | | | | |
| Period | P1 | P2 | P3 | P1 | P2 | P3 | | | | | |
| 1 | 0 | 0 | 0 | 150 | 125 | 200 | | | | | |
| 2 | 0 | 0 | 0 | 235 | 105 | 187 | | | | | |
| 3 | 0 | 0 | 0 | 115 | 150 | 195 | | | | | |
| Weight (Kg.) | 708 | 1712 | 2988 | 1500 | 2992 | 4500 | | | | | |
| Total Weights | | | 14 | 4400 | | | | | | | |

4.2 EXAMPLE 2

4.2.1 EXAMPLE 2: INPUTS

Demand patterns are assumed for all customers as shown in Table 13.

Table 13: Demand of each customer in each period for each product.

| Table 13. Demand of each customer in each period for each product. |
|--|
| Required Demand |

| Period | Customer 1 | | | C | ustomei | : 2 | Customer 3 | | | Cı | Customer 4 | | |
|--------|------------|-----|-----|-----|---------|-----|------------|-----|-----|-----|------------|-----|--|
| renou | P1 | P2 | Р3 | P1 | P2 | Р3 | P1 | P2 | Р3 | P1 | P2 | Р3 | |
| 1 | 450 | 480 | 510 | 450 | 480 | 510 | 450 | 480 | 510 | 450 | 480 | 510 | |
| 2 | 460 | 490 | 520 | 460 | 490 | 520 | 460 | 490 | 520 | 460 | 490 | 520 | |
| 3 | 470 | 500 | 530 | 470 | 500 | 530 | 470 | 500 | 530 | 470 | 500 | 530 | |

4.2.2 EXAMPLE 2: OUTPUTS AND DISCUSSION

The resulted optimal network is as shown in Figure 5.

Figure 5: The resulted optimal network of example 2.

Total profit, total cost, total revenue, and their elements are given in Table 14. Only the inventory holding cost equals zero which means that there is no inventory at all in the network.

Table 14: Total profit, total cost, total revenue, and their elements.

| Revenue | Value | Cost | Value | Cost | Value |
|------------------|-----------|------------------------|------------|----------------------|---------|
| First Sales | 2,666,000 | Fixed Cost | 206,500 | Purchasing Costs | 266,600 |
| Second Sales | 853,120 | Material Cost | 357,600 | Disassembly Cost | 53,640 |
| Recycling Profit | 4,390 | Manufacturing Cost | 377,200 | Remanufacturing Cost | 79,980 |
| | | Non-Utilized Cost | 262,820 | Repairing Cost | 44,700 |
| | | Shortage Cost | 1,200 | Disposal Cost | 1,788 |
| | | Inventory Holding Cost | 0 | Transportation Costs | 28,589 |
| Total Revenue | 3,523,510 | Т | Total Cost | 1,680,617 | |
| | | Total Profit | 1,842,893 | 3 | |

Where the quantities of batches transferred from suppliers to the factories and from factories to distributors are shown in Table 15. Flow balancing is noticed in Table 15 where the total weights of transferred materials are the same of 35760 kg.

Table 15: Number of batches transferred from suppliers and factories.

| From | \$ | Suppliers | Factories | | | |
|--------|----|-----------|-----------|----|----|----|
| FIOIII | S1 | S2 | S3 | F1 | F2 | F3 |

| Period | RM | RM | RM | P1 | P2 | P3 | P1 | P2 | Р3 | P1 | P2 | P3 | |
|----------|-----------------------|-------|-------|------|-------|------|------|------|------|------|------|------|--|
| 1 | 3760 | 4000 | 4000 | 450 | 890 | 510 | 899 | 70 | 987 | 451 | 960 | 543 | |
| 2 | 4000 | 4000 | 4000 | 920 | 490 | 700 | 0 | 710 | 860 | 920 | 760 | 520 | |
| 3 | 4000 | 4000 | 4000 | 471 | 500 | 843 | 938 | 1000 | 354 | 471 | 500 | 843 | |
| Weight | 11760 | 12000 | 12000 | 1841 | 3760 | 6159 | 1837 | 3560 | 6603 | 1842 | 4440 | 5718 | |
| Total W. | Total W. 35760 | | | | 35760 | | | | | | | | |

The number of batches transferred from distributors to customers for all products in all period of also 35760 kg is shown in Table 16

Table 16: Number of batches transferred from distributors to customers.

| | Given Quantities | | | | | | | | | | | | | |
|----------------------|------------------|-------|------|------|---------|------|------|---------|------|------|------------|------|--|--|
| Daviad | Period Cu | | | Cı | ıstomeı | : 2 | Cı | ıstomeı | : 3 | Cı | Customer 4 | | | |
| Period | P1 | P2 | P3 | P1 | P2 | P3 | P1 | P2 | Р3 | P1 | P2 | Р3 | | |
| 1 | 450 | 480 | 510 | 450 | 480 | 510 | 450 | 480 | 510 | 450 | 480 | 510 | | |
| 2 | 460 | 490 | 520 | 460 | 490 | 520 | 460 | 490 | 520 | 460 | 490 | 520 | | |
| 3 | 470 | 500 | 530 | 470 | 500 | 530 | 470 | 500 | 530 | 470 | 500 | 450 | | |
| Weight (Kg.) | 1380 | 2940 | 4680 | 1380 | 2940 | 4680 | 1380 | 2940 | 4680 | 1380 | 2940 | 4440 | | |
| Total Weights | | 35760 | | | | | | | | | | | | |

The shortage can be calculated easily by subtracting given quantities shown in Table 16 from the required quantities (demand) shown in Table 13 and it is shown in Table 17. Table 17 shows that all shortages occurred only on the third product for the fourth (the furthest) customer because the network capacity is lower than the required as shown in Figure 7 and this shortage resulted in a shortage cost of 1200 as shown in Table 14.

Table 17: Shortages.

| Shortage | | | | | | | | | | | | |
|---------------|-----------------------|----|----|----|----|-------|-----|----|-------|------|----|-----|
| Period | Customer 1 Customer 2 | | | | Cu | stome | r 3 | C | ustom | er 4 | | |
| renou | P1 | P2 | P3 | P1 | P2 | P3 | P1 | P2 | P3 | P1 | P2 | Р3 |
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 2 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 80 |
| Weight (Kg.) | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 240 |
| Total Weights | 240 | | | | | | | | | | | |

Figure 6 depicts the given quantities versus demand for all customer and all products. It can be noticed that they are all not equal which means that there is a final shortage for customer 4 from product 3. Figure 7 shows that the total required weights is more than the network capacity in the third period, equals it at the second period, and less than it at the first period which explains final shortage.

Figure 6: Given quantities versus demand for all customer and all products.

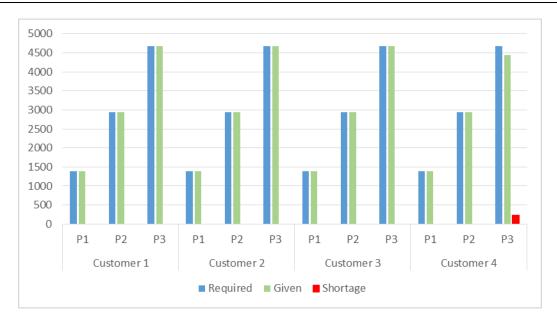
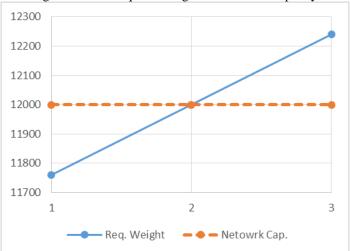


Figure 7: Total required weights vs. network capacity



The flow in the reverse direction begins by receiving the returned products from the first customers by disassembly locations. Table 18 gives the maximum flow weights and the actual flow weights. It is noticed that the disassembly locations receives the maximum flow weights of 17880 kg. So, other actual weights of the repaired, recycled, remanufactured, disposed and redistributed equal the maximum flow weights. The number of products of 17880 kg weight purchased by disassembly locations from the first customers is shown in Table 19.

Table 18: Maximum and actual flow weights.

| | Ratio | Max. fl | ow weights | Actual flow weights | | | | | | | |
|----------------|-------|---------|------------|---------------------|-------|--|--|--|--|--|--|
| Returned | 0.5 | 1 | 7880 | 1 | 7880 | | | | | | |
| Redistributed | 0.8 | 1 | 4304 | 1- | 4304 | | | | | | |
| Repaired | 0.5 | 8940 | | 8940 | | | | | | | |
| Recycled | 0.1 | 1788 | 17880 | 1788 | 17880 | | | | | | |
| Remanufactured | 0.3 | 5364 | 17000 | 5364 | 17860 | | | | | | |
| Disposed | 0.1 | 1788 | | 1788 | | | | | | | |

Table 19: Number of products purchased by disassembly locations from the first customers.

| Tuble 19. Tvuille | | ed Quantities | the first editoriers. |
|-------------------|------|---------------|-----------------------|
| To | | | A3 |
| Period | C1A1 | C1A2 | C1A3 |

| | P1 | P2 | Р3 | P1 | P2 | Р3 | P1 | P2 | Р3 |
|---------------|-----|------|------|------|-------|------|-----|------|------|
| 1 | 225 | 240 | 255 | 0 | 0 | 0 | 0 | 0 | 0 |
| 2 | 230 | 245 | 260 | 0 | 0 | 0 | 0 | 0 | 0 |
| 3 | 235 | 250 | 265 | 0 | 0 | 0 | 0 | 0 | 0 |
| Dowled. | | C2A1 | | | C2A2 | | | C2A3 | |
| Period | P1 | P2 | Р3 | P1 | P2 | Р3 | P1 | P2 | Р3 |
| 1 | 0 | 0 | 0 | 225 | 240 | 255 | 0 | 0 | 0 |
| 2 | 0 | 0 | 0 | 230 | 245 | 260 | 0 | 0 | 0 |
| 3 | 0 | 0 | 0 | 235 | 250 | 265 | 0 | 0 | 0 |
| Period | | C3A1 | | | C3A2 | | | C3A3 | |
| 1 eriou | P1 | P2 | Р3 | P1 | P2 | Р3 | P1 | P2 | Р3 |
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 225 | 240 | 255 |
| 2 | 0 | 0 | 0 | 0 | 0 | 0 | 230 | 245 | 260 |
| 3 | 0 | 0 | 0 | 0 | 0 | 0 | 235 | 250 | 265 |
| Period | | C4A1 | | | C4A2 | | | C4A3 | |
| 1 eriou | P1 | P2 | Р3 | P1 | P2 | Р3 | P1 | P2 | Р3 |
| 1 | 5 | 90 | 115 | 5 | 60 | 135 | 215 | 90 | 5 |
| 2 | 0 | 85 | 110 | 230 | 135 | 0 | 0 | 25 | 150 |
| 3 | 15 | 100 | 85 | 215 | 0 | 85 | 5 | 150 | 55 |
| Weight (Kg.) | 710 | 2020 | 3270 | 1140 | 1860 | 3000 | 910 | 2000 | 2970 |
| Total Weights | | | | | 17880 | | | | |

The number and weights of remanufactured, repaired, and delivered to the second customers matching Table 18 are presented in Tables 20, 21 and 22 respectively.

Table 20: Flow of remanufactured products from factories to redistributors.

| | | Remanufactured | | | | | | | | | | |
|---------------|-----|----------------|------|-----|------|------|----|-----|----|--|--|--|
| Period | | F1R | | | F2R | | | F3R | | | | |
| reriou | P1 | P2 | Р3 | P1 | P2 | Р3 | P1 | P2 | Р3 | | | |
| 1 | 105 | 103 | 131 | 165 | 155 | 175 | 0 | 30 | 0 | | | |
| 2 | 121 | 119 | 147 | 155 | 175 | 165 | 0 | 0 | 0 | | | |
| 3 | 127 | 125 | 141 | 155 | 175 | 165 | 0 | 0 | 0 | | | |
| Weight (Kg.) | 353 | 694 | 1257 | 475 | 1010 | 1515 | 0 | 60 | 0 | | | |
| Total Weights | | 5364 | | | | | | | | | | |

Table 21: Flow of repaired products from disassembly locations to redistributors.

| | Repaired | | | | | | | | |
|----------------------|----------|------|------|-----|-----|------|-----|-----|------|
| Period | A1R | | | A2R | | | A3R | | |
| | P1 | P2 | P3 | P1 | P2 | P3 | P1 | P2 | P3 |
| 1 | 115 | 165 | 185 | 115 | 150 | 195 | 220 | 165 | 130 |
| 2 | 115 | 165 | 185 | 230 | 190 | 130 | 115 | 135 | 205 |
| 3 | 125 | 175 | 175 | 225 | 125 | 175 | 120 | 200 | 160 |
| Weight (Kg.) | 355 | 1010 | 1635 | 570 | 930 | 1500 | 455 | 500 | 1485 |
| Total Weights | 8940 | | | | | | | | |

The number of batches transferred to the second customer through the reverse chain is shown in Table 22.

Second Products K1 To **K2** R1K1 R1K2 Period **P1 P3 P1 P2 P2 P3** 220 268 316 0 0 0 1 2 284 0 0 236 332 0 3 252 300 316 0 0 0 R2K2 R2K1 **Period P1 P2 P3 P1 P2 P3** 0 0 0 280 305 370 2 0 0 0 295 385 365 3 0 0 0 380 300 340 R3K1 R3K2 **Period P1 P2 P3 P1 P2 P3** 1 0 0 0 220 195 130 0 2 0 0 115 135 205 0 0 3 0 120 200 160 708 1704 2892 1500 3000 4500 Weight (Kg.) **Total Weights** 14304

Table 22: Flow of refurbished products from redistributors to second customers.

V. CONCLUSION

From the previous study, the following conclusions can be derived:

- 1. The proposed model is successful in designing forward-reverse logistics networks while considering multi-product in multi-period with three echelons (suppliers, factories and distributors) in the forward direction and two echelons (disassemblies and re-distributors) in the reverse direction.
- 2. Quality level of the returned products, return rate, and others may be tackled as random value, but it is assumed as a deterministic to facilitate discussion.
- 3. This model can be developed easily to match a wide range of practical cases.

It is recommended to:

- 4. Take the time value of money into consideration.
- 5. Tackle the robustness of environmental parameters.
- 6. Take the percent defective of each facility into consideration.

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